

Bethe - Bloch ionization formula

$$-\frac{dE}{dx} = 4\pi N_A r_e^2 m_e c^2 z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\ln \left(\frac{2m_e c^2 \beta^2}{I \cdot (1 - \beta^2)} \right) - \beta^2 - \frac{\delta}{2} \right],$$

N_A = Avogadro number = $6.022 \cdot 10^{23} \text{ mol}^{-1}$

r_e = classical electron radius = $2.818 \times 10^{-15} \text{ m}$

m_e = electron mass = $0.511 \text{ MeV}/c^2$

z = charge number of penetrating particle

Z = atomic mass of absorber

A = atomic number of absorber ($\text{g} \cdot \text{mol}^{-1}$)

δ = density effect correction

I = mean ionization energy $\sim 16 \cdot Z^{0.9} \text{ eV}$